4.1
a. narrow, needle-like leaves; evergreens; conifers
b. broadleafed; deciduous
c. softwoods

4.2
See Fig. 4.4.
a. Annual Ring – wood cells developed on the outside of the tree in one growing season
b. Latewood (summerwood) – smaller, darker, more dense, from late in growing season
   Earlywood (springwood) – larger, light color, less dense, from early in growing season
c. Heartwood – at center of log; inactive cells; collects deposits as aged; darker
   Sapwood – outer, living, active cells; stores food and transports water

4.3
a. Amount of water expressed as percent of dry weight of wood material:
   \[ MC = \frac{\text{moistweight} - \text{ovendryweight}}{\text{ovendryweight}} \times 100\% \]
   b. FSP = MC at point of “no free water” and fully saturated (bound water) wood.
   c. EMC = MC wood assumes in service for a given set of atmospheric conditions

4.4
a. \( MC \leq 19\% \)
b. \( MC > 19\% \)
   Note: These values are for sawn lumber; for glulam see Chap. 5 (dry MC < 16%).

4.5
EMC for buildings in “dry southwest states” is approximately 9%, ranging from 7% to 12% (Ref. 4.7)

4.6
National Design Specification for Wood Construction (NDS)
Design Values for Wood Construction (NDS Design Values Supplement)
Special Design Provisions for Wind & Seismic (NDS Wind & Seismic Supplement)
Commentary on the National Design Specification for Wood Construction (NDS Commentary)
ASD/LRFD Manual for Engineered Wood Construction
4.7 a. NDS Design Values Supplement (provides design values for sawn lumber and glued laminated timber); Wind & Seismic Supplement (provides design guidelines and unit shear capacities for wood shearwalls and diaphragms resisting lateral wind and seismic loads).
  b. The Wind & Seismic Supplement is separated from the NDS and the NDS Design Values Supplement due to the unique requirements for wind-resistant and seismic-resistant design.

4.8

<table>
<thead>
<tr>
<th>Nominal Size</th>
<th>Dressed (in. x in.)</th>
<th>Area (in²)</th>
<th>Iₓ (in⁴)</th>
<th>Sᵧ (in³)</th>
<th>Iᵧ (in⁴)</th>
<th>Sₓ (in³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 2 x 4</td>
<td>1.5 x 3.5</td>
<td>5.25</td>
<td>5.359</td>
<td>3.063</td>
<td>0.984</td>
<td>1.313</td>
</tr>
<tr>
<td>b. 8 x 8</td>
<td>7.5 x 7.5</td>
<td>56.25</td>
<td>263.7</td>
<td>70.31</td>
<td>263.7</td>
<td>70.31</td>
</tr>
<tr>
<td>c. 4 x 10</td>
<td>3.5 x 9.25</td>
<td>32.38</td>
<td>230.8</td>
<td>49.91</td>
<td>33.05</td>
<td>18.89</td>
</tr>
<tr>
<td>d. 6 x 16</td>
<td>5.5 x 15.5</td>
<td>85.25</td>
<td>1707</td>
<td>220.2</td>
<td>214.9</td>
<td>78.15</td>
</tr>
</tbody>
</table>

4.9 a. Nominal 2 to 4 in. thick; any width; practically 2 x 2 to 4 x 16.
  b. Minimum nominal dimension of 5 in. or larger; includes beams & stringers (width more than 2 in. > thickness) and posts & timbers (square; not more than 2 in. out of square).
  c. Design values for the main size categories are determined following different procedures.
     Dimension Lumber- In-grade test program: ASTM D1990.
     Timbers – small clears: ASTM D2555 & D245
     Dimension Lumber: NDS Supplement Tables 4A, 4B, 4C, 4F
     Timbers: NDS Supplement Table 4D

4.10 a. Timbers; 5 in. and thicker, width more than 2 in. > thickness
  b. Dimension Lumber; 2 to 4 in. thick, 2 to 4 in. wide
  c. Dimension Lumber; 2 to 4 in. thick, 4 in. and wider
  d. Dimension Lumber, 2 to 4 in. thick, 5 in. and wider
  e. Timbers; 5 in. and thicker, width not more than 2 in. > thickness
  f. Dimension Lumber; 2 to 4 in. thick, 2 to 4 in. wide
  g. Dimension Lumber; 2 to 4 in. thick, 2 in. and wider, ≤ 10 ft long

4.11 Visually graded is graded visually by inspecting and marking each piece. NDS Supplement Tables 4A, 4B, 4D, 4E, and 4F
  MSR refers to lumber graded mechanically by subjecting each piece to a nondestructive test that measure E about the weak axis. A visual check is also included. NDS Supplement Table 4C
4.12 Visually graded sawn lumber other than Southern Pine

<table>
<thead>
<tr>
<th>Size</th>
<th>Size Category</th>
<th>NDS Supplement</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 10 x 12</td>
<td>P &amp; T</td>
<td>Table 4D</td>
</tr>
<tr>
<td>b. 14 x 14</td>
<td>P &amp; T</td>
<td>Table 4D</td>
</tr>
<tr>
<td>c. 4 x 8</td>
<td>Dimension</td>
<td>Table 4A</td>
</tr>
<tr>
<td>d. 4 x 4</td>
<td>Dimension</td>
<td>Table 4A</td>
</tr>
<tr>
<td>e. 2 x 12</td>
<td>Dimension</td>
<td>Table 4A</td>
</tr>
<tr>
<td>f. 6 x 12</td>
<td>B &amp; S</td>
<td>Table 4D</td>
</tr>
<tr>
<td>g. 8 x 12</td>
<td>B &amp; S</td>
<td>Table 4D</td>
</tr>
<tr>
<td>h. 8 x 10</td>
<td>P &amp; T</td>
<td>Table 4D</td>
</tr>
</tbody>
</table>

4.13 Visually graded sawn lumber – Southern Pine

<table>
<thead>
<tr>
<th>Size</th>
<th>Size Category</th>
<th>NDS Supplement</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. 10 x 12</td>
<td>P &amp; T</td>
<td>Table 4D</td>
</tr>
<tr>
<td>b. 14 x 14</td>
<td>P &amp; T</td>
<td>Table 4D</td>
</tr>
<tr>
<td>c. 4 x 8</td>
<td>Dimension</td>
<td>Table 4B</td>
</tr>
<tr>
<td>d. 4 x 4</td>
<td>Dimension</td>
<td>Table 4B</td>
</tr>
<tr>
<td>e. 2 x 12</td>
<td>Dimension</td>
<td>Table 4B</td>
</tr>
<tr>
<td>f. 6 x 12</td>
<td>B &amp; S</td>
<td>Table 4D</td>
</tr>
<tr>
<td>g. 8 x 12</td>
<td>B &amp; S</td>
<td>Table 4D</td>
</tr>
<tr>
<td>h. 8 x 10</td>
<td>P &amp; T</td>
<td>Table 4D</td>
</tr>
</tbody>
</table>

4.14 Stress grades of visually graded Hem-Fir

a. Dimension Lumber (NDS Supplement Table 4A)
   Select Structural; No.1 & Btr; No.1; No.2; No.3; Stud; Construction;
   Standard; Utility
b. Beams and Stringers (NDS Supplement Table 4D)
   Select Structural; No.1; No.2
c. Posts and Timbers (NDS Supplement Table 4D)
   Select Structural; No.1; No.2
4.15 Stress grades of visually graded Southern Pine

a. Dimension Lumber-stress grades vary with size (NDS Supplement Table 4B)

<table>
<thead>
<tr>
<th>Thickness</th>
<th>Stress Grades</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 in. – 4 in. thick</td>
<td>Dense Select Structural; Select Structural;</td>
</tr>
<tr>
<td></td>
<td>Non-Dense Select Structural; No. 1 Dense; No. 1 Non-</td>
</tr>
<tr>
<td></td>
<td>Dense; No. 2 Dense; No. 2; No. 2 Non-Dense;</td>
</tr>
<tr>
<td></td>
<td>No. 3 and Stud</td>
</tr>
<tr>
<td>2 in. – 4 in. thick</td>
<td>Construction; Standard; Utility</td>
</tr>
<tr>
<td>4 in. wide</td>
<td></td>
</tr>
<tr>
<td>2 – 4 in. thick</td>
<td>Dense Structural 86;</td>
</tr>
<tr>
<td>2 in. and wider</td>
<td>Dense Structural 72;</td>
</tr>
<tr>
<td></td>
<td>Dense Structural 65</td>
</tr>
</tbody>
</table>

b. Beams & Stringers and c. Posts & Timbers (NDS Supplement Table 4D)

<table>
<thead>
<tr>
<th>Thickness</th>
<th>Stress Grades</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 in. x 5 in. and larger</td>
<td>Dense Select Structural; Select Structural;</td>
</tr>
<tr>
<td></td>
<td>No. 1 Dense; No. 1;</td>
</tr>
<tr>
<td></td>
<td>No. 2 Dense; No. 2;</td>
</tr>
<tr>
<td></td>
<td>Dense Structural 86;</td>
</tr>
<tr>
<td></td>
<td>Dense Structural 72;</td>
</tr>
<tr>
<td></td>
<td>Dense Structural 65</td>
</tr>
</tbody>
</table>
4.16 Reference design values for No. 1 DF-L

**Dimension Lumber** (NDS Supplement Table 4A)

- c. 4 x 16 – Dimension Lumber
- d. 4 x 4 – Dimension Lumber
- e. 2 x 10 – Dimension Lumber

\[
\begin{align*}
F_b &= 1000 \text{ psi} \\
F_t &= 675 \text{ psi} \\
F_v &= 180 \text{ psi} \\
F_c &\perp = 625 \text{ psi} \\
F_c &= 1500 \text{ psi} \\
E &= 1,700,000 \text{ psi} \\
E_{\text{min}} &= 620,000 \text{ psi}
\end{align*}
\]

**Beams and Stringers** (NDS Supplement Table 4D)

- f. 6 x 12 – Beams & Stringers
- h. 10 x 14 – Beams & Stringers

\[
\begin{align*}
F_b &= 1350 \text{ psi} \\
F_t &= 675 \text{ psi} \\
F_v &= 170 \text{ psi} \\
F_c &\perp = 625 \text{ psi} \\
F_c &= 925 \text{ psi} \\
E &= 1,600,000 \text{ psi} \\
E_{\text{min}} &= 580,000 \text{ psi}
\end{align*}
\]

**Posts and Timbers** (NDS Supplement Table 4D)

- a. 10 x 10 – Posts & Timbers
- b. 12 x 14 – Posts & Timbers
- g. 6 x 8 – Posts & Timbers

\[
\begin{align*}
F_b &= 1200 \text{ psi} \\
F_t &= 825 \text{ psi} \\
F_v &= 170 \text{ psi} \\
F_c &\perp = 625 \text{ psi} \\
F_c &= 1000 \text{ psi} \\
E &= 1,600,000 \text{ psi} \\
E_{\text{min}} &= 580,000 \text{ psi}
\end{align*}
\]
4.17 Nominal design values (LRFD) for No. 1 DF-L
Dimension Lumber (NDS Supplement Table 4A)
c. 4 x 16 – Dimension Lumber
d. 4 x 4 – Dimension Lumber
e. 2 x 10 – Dimension Lumber
\[ F_{bn} = F_b(K_F) = 1000 \text{ psi (2.54)} = 2.54 \text{ ksi} \quad (\Phi_b = 0.85) \]
\[ F_{in} = F_i(K_F) = 675 \text{ psi (2.70)} = 1.82 \text{ksi} \quad (\Phi_i = 0.8) \]
\[ F_{vn} = F_v(K_F) = 180 \text{ psi (2.88)} = 0.518 \text{ksi} \quad (\Phi_v = 0.75) \]
\[ F_{c,n} = F_{c,\perp}(K_F) = 625 \text{ psi (2.083)} = 1.30 \text{ksi} \quad (\Phi_c = 0.9) \]
\[ F_{cn} = F_c(K_F) = 1500 \text{ psi (2.40)} = 3.60 \text{ksi} \quad (\Phi_c = 0.9) \]
\[ E = 1,700,000 \text{ psi} \]
\[ E_{\text{min}-n} = E_{\text{min}}(K_F) = 620,000 \text{ psi (1.765)} = 1094 \text{ ksi} \quad (\Phi_s = 0.85) \]

Beams and Stringers (NDS Supplement Table 4D)
f. 6 x 12 – Beams & Stringers

h. 10 x 14 – Beams & Stringers
\[ F_{bn} = F_b(K_F) = 1350 \text{ psi (2.54)} = 3.43 \text{ ksi} \quad (\Phi_b = 0.85) \]
\[ F_{in} = F_i(K_F) = 675 \text{ psi (2.70)} = 1.82 \text{ ksi} \quad (\Phi_i = 0.8) \]
\[ F_{vn} = F_v(K_F) = 170 \text{ psi (2.88)} = 0.490 \text{ ksi} \quad (\Phi_v = 0.75) \]
\[ F_{c,n} = F_{c,\perp}(K_F) = 625 \text{ psi (2.083)} = 1.30 \text{ ksi} \quad (\Phi_c = 0.9) \]
\[ F_{cn} = F_c(K_F) = 925 \text{ psi (2.40)} = 2.22 \text{ ksi} \quad (\Phi_c = 0.9) \]
\[ E = 1,600,000 \text{ psi} \]
\[ E_{\text{min}-n} = E_{\text{min}}(K_F) = 580,000 \text{ psi (1.765)} = 1024 \text{ ksi} \quad (\Phi_s = 0.85) \]

Posts and Timbers (NDS Supplement Table 4D)
a. 10 x 10 – Posts & Timbers
b. 12 x 14 – Posts & Timbers
g. 6 x 8 – Posts & Timbers
\[ F_{bn} = F_b(K_F) = 1200 \text{ psi (2.54)} = 3.05 \text{ ksi} \quad (\Phi_b = 0.85) \]
\[ F_{in} = F_i(K_F) = 825 \text{ psi (2.70)} = 2.23 \text{ ksi} \quad (\Phi_i = 0.8) \]
\[ F_{vn} = F_v(K_F) = 170 \text{ psi (2.88)} = 0.490 \text{ ksi} \quad (\Phi_v = 0.75) \]
\[ F_{c,n} = F_{c,\perp}(K_F) = 625 \text{ psi (2.083)} = 1.30 \text{ ksi} \quad (\Phi_c = 0.9) \]
\[ F_{cn} = F_c(K_F) = 1000 \text{ psi (2.40)} = 2.40 \text{ ksi} \quad (\Phi_c = 0.9) \]
\[ E = 1,600,000 \text{ psi} \]
\[ E_{\text{min}-n} = E_{\text{min}}(K_F) = 580,000 \text{ psi (1.765)} = 1024 \text{ ksi} \quad (\Phi_s = 0.85) \]

4.18

<table>
<thead>
<tr>
<th>Adjustment Factor</th>
<th>Design values that may require adjustment</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. Size Factor (C_P)</td>
<td>(F_b; F_i; F_c)</td>
</tr>
<tr>
<td>b. Time Effect Factor (\lambda)</td>
<td>(F_b; F_i; F_v; F_c; F_{c,\perp})</td>
</tr>
<tr>
<td>c. Load Duration Factor (C_D)</td>
<td>(F_b; F_i; F_v; F_c)</td>
</tr>
<tr>
<td>d. Repetitive Member Factor (C_r)</td>
<td>(F_b)</td>
</tr>
<tr>
<td>e. Temperature Factor (C_t)</td>
<td>(F_b; F_i; F_v; F_c; F_{c,\perp}; E; E_{\text{min}})</td>
</tr>
<tr>
<td>f. Wet Service Factor (C_M)</td>
<td>(F_b; F_i; F_v; F_c; F_{c,\perp}; E; E_{\text{min}})</td>
</tr>
<tr>
<td>g. Flat Use Factor (C_{fu})</td>
<td>(F_b)</td>
</tr>
</tbody>
</table>
4.19

a. Load Duration Factor, $C_D$: The strength of a wood member is affected by the total accumulated length of time that a load is applied. The shorter the duration of load, the higher the strength of a wood member. $C_D$ is the multiplier that adjusts the reference design value from normal duration (10 years) to other durations for ASD. See NDS 2.3.2 and Appendix B.

b. Time Effect Factor, $\lambda$: The strength of a wood member is affected by the total accumulated length of time that a load is applied. $\lambda$ is the multiplier that adjusts the LRFD resistance of wood members to ensure that consistent reliability is achieved for load duration effects in various LRFD load combinations. See NDS Appendix N.

c. Wet Service Factor, $C_M$: The moisture content (MC) of a wood member affects its load capacity. Most reference design values for sawn lumber apply to MC $\leq 19$ percent in service. Higher moisture contents require reduction of design values by $C_M$. The following reference design values are subject to adjustment for increased moisture content: $F_{fb}, F_{ft}, F_{fc\perp}, F_{cv}, E$ and $E_{min}$. See NDS 4.3.3 and the Adjustment Factors sections of NDS Supplement Tables 4A, 4B, 4C, 4D, 4E, and 4F.

d. Size Factor, $C_F$: The size of a wood member affects its strength. For visually graded Dimension Lumber, $C_F$ applies to $F_{fb}, F_{ft}$ and $F_{fc}$. See NDS 4.3.6.1 and the Adjustment Factor section of NDS Supplement Tables 4A and 4F. For Timbers, the size factor applies to $F_{fb}, E$ and $E_{min}$. See NDS 4.3.6.2 and the Adjustment Factors section of NDS Supplement Table 4D. For Decking, $C_F$ applies only to $F_{fb}$. See NDS 4.3.6.4 and the Adjustment Factors section of NDS Supplement Table 4E.

e. Repetitive Member Factor, $C_r$: Applies to Dimension Lumber, but not to Timbers. When three or more wood members are spaced not more that 24 in. o/c and are connected together by a load distributing element (such as sheathing), the bending design value $F_{fb}$ may be increased by $C_r = 1.15$. This is a 15 percent increase over single member bending design values. The $C_r$ adjustment recognizes that failure of a single member in a repetitive application will not mean failure of the overall system. The load will be distributed to other members.

4.20 Wood has the ability to support higher stresses for short periods of time. Both the load duration factor ($C_D$) and the time effect factor ($\lambda$) are employed to adjust wood strength properties based on the duration of applied design loads. The load duration factor ($C_D$) is used to adjust reference design values in allowable stress design (ASD), and is based on the shortest duration load in an ASD load combination. The time effect factor ($\lambda$) is used to adjust nominal design values in load and resistance factor design (LRFD), and is based on the dominant transient load in an LRFD load combination. Time effect factors ($\lambda$) are intended to ensure consistent reliability for load duration effects across various load combinations.
4.21 a. Snow (S): $C_D = 1.15$
b. Wind (W): $C_D = 1.6$
c. Floor Live Load (L): $C_D = 1.0$
d. Roof Live Load (Lr): $C_D = 1.25$
e. Dead Load (D): $C_D = 0.9$

4.22 a. $1.2D + 1.6S + L$: $\lambda = 0.8$
b. $1.2D + 1.6W + L + 0.5S$: $\lambda = 1.0$
c. $1.2D + 1.6L + 0.5S$: $\lambda = 0.8$ (for L due to occupancy)
d. $1.2D + 1.6L_r + L$: $\lambda = 0.8$
e. $1.4D$: $\lambda = 0.6$

4.23 Compression perpendicular to grain ($F_{bc} \parallel$), average modulus of elasticity ($E$), and reduced modulus of elasticity for stability calculations ($E_{min}$) are not adjusted by $C_D$ in ASD calculations. Average modulus of elasticity ($E$) and reduced modulus of elasticity for stability calculations ($E_{min}$) are not adjusted by $\lambda$ in LRFD calculations.

4.24 Most reference design values apply to dry service conditions*. Dry service conditions are defined as:
   a. Sawn Lumber $MC \leq 19$ percent
   b. Glulam $MC < 16$ percent
When the moisture content exceeds these limits, the reference design values are reduced by a wet service factor $C_M$ that is less than 1.0

* Southern Pine has $C_M$ included in some of the reference design values (NDS Supplement Table 4B). Many of the reference design values for Timbers (NDS Supplement Table 4D) have already been adjusted for $C_M$.

4.25 The load capacity of wood decreases as the temperature increases. Reductions in strength caused by heating up to 150 degrees F are generally reversible when the temperature returns to normal. Reductions in strength may not be reversible when heating exceeds 150 degrees F. Reduction in strength occurs when the member is subjected to the full design capacity.
When a wood member is consistently heated above 100 degrees F and is subjected to the full design load, an adjustment for temperature effects will be required. This may occur in an industrial plant, but reductions are not normally required in ordinary roof structures. See NDS 2.3.3 and Appendix C.
4.26 Pressure preservative treated wood has chemicals impregnated in the treated zone which resist attack by decay, termites and other insects, and marine borers. Reference design values apply directly to preservative treated wood, and an adjustment factor is not required unless the member has been incised to increase the penetration of preservatives.

Fire-retardant-treated wood has much higher concentrations of chemicals than preservative treated wood. At one time a 10 percent reduction in reference design values was specified. However, the reduction in strength varies with the treating process, and the NDS refers the designer to the company providing the fire retardant treatment for appropriate reduction factors.

NOTE: The performance of fire-retardant-treated wood products has been the subject of considerable concern and litigation.

4.27 Wood that is continuously submerged in fresh water will not decay and does not need to be preservative treated. However, wood that is partially submerged, or wood that undergoes cycles of submersion followed by exposure to the atmosphere, should be preservative treated. Wood that is submerged in salt water should be preservative treated to protect from marine borers. Preservative treated wood has an extensive record of resisting attack in both fresh water and salt water environments.

4.28 Critical ASD load combination for a fully braced member

<table>
<thead>
<tr>
<th>ASD Combination</th>
<th>Load</th>
<th>$C_D$</th>
<th>Load/$C_D$</th>
</tr>
</thead>
<tbody>
<tr>
<td>D (roof + floor)</td>
<td>6 + 3 = 9 k</td>
<td>0.9</td>
<td>10 k</td>
</tr>
<tr>
<td>D + L</td>
<td>9 + 10 = 19 k</td>
<td>1</td>
<td>19 k</td>
</tr>
<tr>
<td>D + $L_t$</td>
<td>9 + 5 = 14 k</td>
<td>1.25</td>
<td>11.2 k</td>
</tr>
<tr>
<td>D + W</td>
<td>9 + 10 = 19 k</td>
<td>1.6</td>
<td>11.9 k</td>
</tr>
<tr>
<td>D + 0.75($L + L_t$)</td>
<td>9 + 0.75(10 + 5) = 20.25 k</td>
<td>1.25</td>
<td>16.2 k</td>
</tr>
<tr>
<td>D + 0.75($W + L + L_t$)</td>
<td>9 + 0.75(10 + 10 + 5) = 27.75 k</td>
<td>1.6</td>
<td>17.3 k</td>
</tr>
</tbody>
</table>

* The largest load in this column defines the critical ASD load combination for a fully braced member: D + L

Note: Actual loads (i.e., loads that have not been divided by $C_D$) should be used in design calculations. The load duration factor should then be used to adjust the appropriate reference design values. In this problem, the actual critical load is 19 k and $C_D = 1.0$. The above analysis is used to define the critical combination only for fully braced members, tension members, or connections.
4.29 Critical ASD load combination for a fully braced member

\[ W = 10 \text{ k} \] > \[ 0.7E = 0.7(12 \text{ k}) = 8.4 \text{ k} \]
\[ S = 18 \text{ k} \] > \[ L_r = 7 \text{ k} \]

<table>
<thead>
<tr>
<th>Combination</th>
<th>Load</th>
<th>( C_D )</th>
<th>Load/( C_D )*</th>
</tr>
</thead>
<tbody>
<tr>
<td>D (roof + floor)</td>
<td>5 + 6 = 11 k</td>
<td>0.9</td>
<td>12.2 k</td>
</tr>
<tr>
<td>D + L</td>
<td>11 + 15 = 26 k</td>
<td>1</td>
<td>26.0 k</td>
</tr>
<tr>
<td>D + S</td>
<td>11 + 18 = 29 k</td>
<td>1.15</td>
<td>25.2 k</td>
</tr>
<tr>
<td>D + L_r</td>
<td>11 + 7 = 18 k</td>
<td>1.25</td>
<td>14.4 k</td>
</tr>
<tr>
<td>D + 0.75(L + S)</td>
<td>11 + 0.75(15 + 18) = 35.75 k</td>
<td>1.15</td>
<td>31.1 k</td>
</tr>
<tr>
<td>D + 0.75(L + L_r)</td>
<td>11 + 0.75(15 + 7) = 27.5 k</td>
<td>1.25</td>
<td>22.0 k</td>
</tr>
<tr>
<td>D + (W or 0.7E)</td>
<td>11 + 10 = 21 k</td>
<td>1.6</td>
<td>13.1 k</td>
</tr>
<tr>
<td>D + 0.75(W or 0.7E) + 0.75L + 0.75(L_r or S)</td>
<td>11 + 0.75(10 + 15 + 18) = 43.25 k</td>
<td>1.6</td>
<td>27.0 k</td>
</tr>
</tbody>
</table>

* The largest load in this column defines the critical ASD load combination for a fully braced member: \( D + 0.75(L + S) \)

Note: Actual loads (i.e., loads that have not been divided by \( C_D \)) should be used in design calculations. The load duration factor should then be used to adjust the appropriate reference design values. In this problem, the actual critical load is 35.75 k and \( C_D = 1.15 \). The above analysis is used to define the critical combination only for fully braced members, tension members, or connections.
4.30 ASD – Hem-Fir No.2, fully braced; bending about strong axis

a. **2 x 10 joists** at 16 in. o.c. \( (C_r = 1.15) \); D + S load combination \( (C_D = 1.15) \)

\( C_F \) applies for bending, tension and compression; other factors equal to unity

\[ F_{h}^{'} = F_t (C_D)(C_F) = 850 \text{ psi (1.15)(1.1)} = 1237 \text{ psi} \]

\[ F_{i}^{'} = F_t (C_D)(C_F) = 525 \text{ psi (1.15)(1.1)} = 664 \text{ psi} \]

\[ F_{v}^{'} = F_v (C_D) = 150 \text{ psi (1.15)} = 173 \text{ psi} \]

\[ F_{c,\perp}^{'} = F_{c,\perp} (C_D)(C_F) = 405 \text{ psi} \]

\[ F_{c}^{'} = F_c (C_D)(C_F) = 1300 \text{ psi (1.15)(1.0)} = 1495 \text{ psi} \]

**Note that** \( C_F \) **would also apply for column buckling of an axially loaded member.**

\[ E' = E = 1,300,000 \text{ psi} \]

\[ E_{min}^{'} = E_{min} = 470,000 \text{ psi} \]

b. **6 x 14 (Beams & Stringers); supports permanent load \( (C_D = 0.9) \)**

\( C_F = (12/13.5)^{0.111} = 0.987 \) for bending; other factors equal to unity

\[ F_{h}^{'} = F_t (C_D)(C_F) = 675 \text{ psi (0.9)(0.987)} = 600 \text{ psi} \]

\[ F_{i}^{'} = F_t (C_D) = 350 \text{ psi (0.9)} = 315 \text{ psi} \]

\[ F_{v}^{'} = F_v (C_D) = 140 \text{ psi (0.9)} = 126 \text{ psi} \]

\[ F_{c,\perp}^{'} = F_{c,\perp} = 405 \text{ psi} \]

\[ F_{c}^{'} = F_c (C_D) = 500 \text{ psi (0.9)} = 450 \text{ psi} \]

**Note that** \( C_F \) **would also apply for column buckling of an axially loaded member.**

\[ E' = E = 1,100,000 \text{ psi} \]

\[ E_{min}^{'} = E_{min} = 400,000 \text{ psi} \]

c. **4 x 14 purlins** at 8 ft o.c.; D + L_r load combination \( (C_D = 1.25) \)

\( C_F \) applies for bending, tension and compression; other factors equal to unity

\[ F_{h}^{'} = F_t (C_D)(C_F) = 850 \text{ psi (1.25)(1.0)} = 1063 \text{ psi} \]

\[ F_{i}^{'} = F_t (C_D)(C_F) = 525 \text{ psi (1.25)(0.9)} = 591 \text{ psi} \]

\[ F_{v}^{'} = F_v (C_D) = 150 \text{ psi (1.25)} = 188 \text{ psi} \]

\[ F_{c,\perp}^{'} = F_{c,\perp} = 405 \text{ psi} \]

\[ F_{c}^{'} = F_c (C_D)(C_F) = 1300 \text{ psi (1.25)(0.9)} = 1463 \text{ psi} \]

**Note that** \( C_F \) **would also apply for column buckling of an axially loaded member.**

\[ E' = E = 1,300,000 \text{ psi} \]

\[ E_{min}^{'} = E_{min} = 470,000 \text{ psi} \]

d. **4 x 6 beams** at 4 ft o.c.; D + L load combination \( (C_D = 1.0) \); \( C_M \) applies

\( C_F \) applies for bending, tension and compression; other factors equal to unity

\[ F_{h}^{'} = F_t (C_D)(C_M)(C_F) = 850 \text{ psi (1.0)(1.0)(1.3)} = 1105 \text{ psi} \]

\[ C_M = 1.0 \] for bending since \( F_t (C_F) = 1105 \text{ psi} < 1150 \text{ psi} \]

\[ F_{i}^{'} = F_t (C_D)(C_M)(C_F) = 525 \text{ psi (1.0)(1.0)(1.3)} = 683 \text{ psi} \]

\[ F_{v}^{'} = F_v (C_D)(C_M) = 150 \text{ psi (1.0)} = 146 \text{ psi} \]

\[ F_{c,\perp}^{'} = F_{c,\perp} (C_M) = 405 \text{ psi (0.67)} = 271 \text{ psi} \]

\[ F_{c}^{'} = F_c (C_D)(C_M)(C_F) = 1300 \text{ psi (1.0)(0.8)(1.1)} = 1144 \text{ psi} \]

**Note that** \( C_F \) **would also apply for column buckling of an axially loaded member.**

\[ E' = E (C_M) = 1,300,000 \text{ psi (0.9)} = 1,170,000 \text{ psi} \]

\[ E_{min}^{'} = E_{min} (C_M) = 470,000 \text{ psi (0.9)} = 423,000 \text{ psi} \]
4.31 LRFD ($K_F$ and $\Phi$ apply) – Hem-Fir No. 2, fully braced; bending about strong axis

a. 2 x 10 joists at 16 in. o.c. ($C_r = 1.15$); 1.2D + 1.6S load combination ($\lambda = 0.8$)

$C_F$ applies for bending, tension and compression; other factors equal to unity

$A = 13.88$ in$^2$; $S_i = 21.39$ in$^3$

**Bending moment**

$F_{bn} = F_h (K_F) = 850$ psi ($2.54$) = 2159 psi = 2.16 ksi

$F_{bn}' = F_{bn} (\Phi_h)(\lambda)(C_F)(C_r) = 2.16$ ksi ($0.85)(0.8)(1.1) = 1.86$ ksi

$M_n' = F_{bn}' (S_i) = 1.86$ ksi ($21.39$ in$^3$) = 39.7 k-in.

**Tension**

$F_{in} = F_i (K_F) = 525$ psi ($2.7$) = 1418 psi = 1.42 ksi

$F_{in}' = F_{in} (\Phi_i)(\lambda)(C_F) = 1.42$ ksi ($0.8)(0.8)(1.1) = 0.998$ k

$T_n' = F_{in}' (A) = 0.998$ ksi ($13.88$ in$^2$) = 13.9 k

**Flexural Shear**

$F_{vn} = F_v (K_F) = 150$ psi ($2.88$) = 432 psi = 0.432 k

$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.432$ ksi ($0.75)(0.8) = 0.259$ k

$V_n = F_{vn}' (2/3)(A) = 0.259$ ksi ($2/3)(13.88$ in$^2$) = 2.4 k

**Compression perpendicular to grain (bearing)**

$F_{cn} = F_c (K_F) = 405$ psi ($2.083$) = 844 psi = 0.844 k

$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 0.844$ ksi ($0.9)(0.8) = 0.607$ k

**Compression parallel to grain**

$F_{cn} = F_c (K_F) = 1300$ psi ($2.4$) = 3120 psi = 3.12 k

$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 3.12$ ksi ($0.9)(0.8)(1.0) = 2.25$ k

$P_n = F_{cn}' (A) = 2.25$ ksi ($13.88$ in$^2$) = 31.2 k

**Note that $C_F$ would also apply for column buckling of an axially loaded member.**

**Modulus of Elasticity**

$E = 1,300,000$ psi = 1300 ksi

$E_{min-n} = E_{min} (K_F) = 470,000$ psi ($1.765$) = 829,550 psi = 830 ksi

$E_{min-n}' = E_{min-n} (\Phi_i) = 830$ ksi ($0.85) = 705$ k

b. 6 x 16 (Beams & Stringers); 1.2D + 1.6L (storage) load ($\lambda = 0.7$)

$C_F = (12/15.5)^{0.111} = 0.972$ for bending; other factors equal to unity

$A = 85.25$ in$^2$; $S_i = 220.2$ in$^3$

**Bending moment**

$F_{bn} = F_h (K_F) = 675$ psi ($2.54$) = 1714.5 psi = 1.71 k

$F_{bn}' = F_{bn} (\Phi_h)(\lambda)(C_F) = 1.71$ ksi ($0.85)(0.7)(0.972) = 0.992$ k

$M_n' = F_{bn}' (S_i) = 0.992$ kisi ($220.2$ in$^3$) = 218 k-in.

**Tension**

$F_{in} = F_i (K_F) = 350$ psi ($2.7$) = 945 psi = 0.945 k

$F_{in}' = F_{in} (\Phi_i)(\lambda) = 0.945$ ksi ($0.8)(0.7) = 0.529$ k

$T_n' = F_{in}' (A) = 0.529$ ksi ($85.25$ in$^2$) = 45.1 k

**Flexural Shear**

$F_{vn} = F_v (K_F) = 140$ psi ($2.88$) = 403 psi = 0.403 k

$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.403$ ksi ($0.75)(0.7) = 0.212$ k

$V_n = F_{vn}' (2/3)(A) = 0.212$ ksi ($2/3)(85.25$ in$^2$) = 12.0 k
Compression perpendicular to grain (bearing)

\[ F_{c_{bn}} = F_c (K_F) = 405 \text{ psi (2.083)} = 844 \text{ psi} = 0.844 \text{ ksi} \]
\[ F_{c_{bn}'} = F_{c_{bn}} (\Phi_c (\lambda)) = 0.844 \text{ ksi (0.9)(0.7)} = 0.531 \text{ ksi} \]

Compression parallel to grain

\[ F_{cn} = F_c (K_F) = 500 \text{ psi (2.4)} = 1200 \text{ psi} = 1.20 \text{ ksi} \]
\[ F_{cn} = F_{cn} (\Phi_c (\lambda)) = 1.20 \text{ ksi (0.9)(0.7)} = 0.756 \text{ ksi} \]
\[ P_n' = F_{cn}' (A) = 0.756 \text{ ksi (85.25 in}^2\text{)} = 64.4 \text{ k} \]

Note that \( C_F \) would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

\[ E' = E = 1,100,000 \text{ psi} = 1100 \text{ ksi} \]
\[ E_{min-n} = E_{min} (K_F) = 400,000 \text{ psi (1.765)} = 706,000 \text{ psi} = 706 \text{ ksi} \]
\[ E_{min-n}' = E_{min-n} (\Phi_s) = 706 \text{ ksi (0.85)} = 600 \text{ ksi} \]

4 x 14 purlins at 8 ft o.c.; 1.2D + 1.6L, load combination (\( \lambda = 0.8 \))

\[ C_F \] applies for bending, tension and compression; other factors equal to unity

\[ A = 46.38 \text{ in}^2; S_t = 102.4 \text{ in}^3 \]

Bending moment

\[ F_{bn} = F_h (K_F) = 850 \text{ psi (2.54)} = 2159 \text{ psi} = 2.16 \text{ ksi} \]
\[ F_{bn}' = F_{bn} (\Phi_h (\lambda) (C_F) = 2.16 \text{ ksi (0.85)(0.8)(1.0)} = 1.47 \text{ ksi} \]
\[ M_n' = F_{bn}' (S_c) = 1.47 \text{ ksi (102.4 in}^3\text{)} = 150 \text{ k-in.} \]

Tension

\[ F_{tn} = F_t (K_F) = 525 \text{ psi (2.7)} = 1418 \text{ psi} = 1.42 \text{ ksi} \]
\[ F_{tn}' = F_{tn} (\Phi_t (\lambda) (C_F) = 1.42 \text{ ksi (0.8)(0.8)(0.9)} = 0.816 \text{ ksi} \]
\[ T_n = F_{tn}' (A) = 0.816 \text{ ksi (46.38 in}^2\text{)} = 37.9 \text{ k} \]

Flexural Shear

\[ F_{vn} = F_v (K_F) = 150 \text{ psi (2.88)} = 432 \text{ psi} = 0.432 \text{ ksi} \]
\[ F_{vn}' = F_{vn} (\Phi_v (\lambda) = 0.432 \text{ ksi (0.75)(0.8)} = 0.259 \text{ ksi} \]
\[ V_n' = F_{vn}' (2/3)(A) = 0.259 \text{ ksi (2/3)(46.38 in}^2\text{)} = 8.0 \text{ k} \]

Compression perpendicular to grain (bearing)

\[ F_{c_{bn}} = F_c (K_F) = 405 \text{ psi (2.083)} = 844 \text{ psi} = 0.844 \text{ ksi} \]
\[ F_{c_{bn}'} = F_{c_{bn}} (\Phi_c (\lambda)) = 0.844 \text{ ksi (0.9)(0.8)} = 0.607 \text{ ksi} \]

Compression parallel to grain

\[ F_{cn} = F_c (K_F) = 1300 \text{ psi (2.4)} = 3120 \text{ psi} = 3.12 \text{ ksi} \]
\[ F_{cn} = F_{cn} (\Phi_c (\lambda) (C_F) = 3.12 \text{ ksi (0.9)(0.8)(0.9)} = 2.02 \text{ ksi} \]
\[ P_n' = F_{cn}' (A) = 2.02 \text{ ksi (46.38 in}^2\text{)} = 93.8 \text{ k} \]

Note that \( C_F \) would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

\[ E' = E = 1,300,000 \text{ psi} = 1300 \text{ ksi} \]
\[ E_{min-n} = E_{min} (K_F) = 470,000 \text{ psi (1.765)} = 829,550 \text{ psi} = 830 \text{ ksi} \]
\[ E_{min-n}' = E_{min-n} (\Phi_s) = 830 \text{ ksi (0.85)} = 705 \text{ ksi} \]
d. **4 x 6 beams** at 4 ft o.c.; 1.2D + 1.6L (occupancy) load \((\lambda = 0.8)\); \(C_F\) applies for bending, tension and compression; other factors equal to unity \(A = 19.25\,\text{in}^2;\) \(S_t = 17.65\,\text{in}^3\)

**Bending moment**

\[ F_{bn} = F_b \cdot (K_F) = 850\,\text{psi} \cdot (2.54) = 2159\,\text{psi} = 2.16\,\text{ksi} \]

\( C_B M_B\) applies for bending, tension and compression; other factors equal to unity

\[
F_{bn}^* = F_{bn} \cdot (\Phi_b)(\lambda)(C_M)(C_F) = 2.16\,\text{ksi} (0.85)(0.8)(1.0)(1.3) = 1.91\,\text{ksi} \\
M_n^* = F_{bn}^* \cdot (S_t) = 1.91\,\text{ksi} (17.65\,\text{in}^3) = 33.7\,\text{k-in}. \\
\]

**Tension**

\[ F_{tn} = F_t \cdot (K_F) = 525\,\text{psi} \cdot (2.7) = 1418\,\text{psi} = 1.42\,\text{ksi} \]

\[ F_{tn}^* = F_{tn} \cdot (\Phi_t)(\lambda)(C_M)(C_F) = 1.42\,\text{ksi} (0.8)(0.8)(1.0)(1.3) = 1.18\,\text{ksi} \\
T_n^* = F_{tn}^* \cdot (A) = 1.18\,\text{ksi} (19.25\,\text{in}^2) = 22.7\,\text{k} \\
\]

**Flexural Shear**

\[ F_{vn} = F_v \cdot (K_F) = 150\,\text{psi} \cdot (2.88) = 432\,\text{psi} = 0.432\,\text{ksi} \]

\[ F_{vn}^* = F_{vn} \cdot (\Phi_v)(\lambda)(C_M)(C_F) = 0.432\,\text{ksi} (0.75)(0.8)(0.97) = 0.251\,\text{ksi} \\
V_n^* = F_{vn}^* \cdot (2/3)(A) = 0.251\,\text{ksi} (2/3)(19.25\,\text{in}^2) = 3.2\,\text{k} \\
\]

**Compression perpendicular to grain (bearing)**

\[ F_{cbn} = F_{cb} \cdot (K_F) = 405\,\text{psi} \cdot (2.083) = 844\,\text{psi} = 0.844\,\text{ksi} \]

\[ F_{cbn}^* = F_{cbn} \cdot (\Phi_c)(\lambda)(C_M)(C_F) = 0.844\,\text{ksi} (0.9)(0.8)(0.67) = 0.407\,\text{ksi} \\
\]

**Compression parallel to grain**

\[ F_{cn} = F_c \cdot (K_F) = 1300\,\text{psi} \cdot (2.4) = 3120\,\text{psi} = 3.12\,\text{ksi} \]

\[ F_{cn}^* = F_{cn} \cdot (\Phi_c)(\lambda)(C_M)(C_F) = 3.12\,\text{ksi} (0.9)(0.8)(0.8)(1.1) = 1.98\,\text{ksi} \\
P_n^* = F_{cn}^* \cdot (A) = 1.98\,\text{ksi} (19.25\,\text{in}^2) = 38.1\,\text{k} \\
\]

**Modulus of Elasticity**

\[
E^* = E \cdot (C_M) = 1,300,000\,\text{psi} (0.9) = 1,170,000 = 1170\,\text{ksi} \\
E_{\text{min-n}} = E_{\text{min}} \cdot (K_F) = 470,000\,\text{psi} (1.765) = 829,550\,\text{psi} = 830\,\text{ksi} \\
E_{\text{min-n}}^* = E_{\text{min-n}} \cdot (\Phi_i)(C_M)(C_F) = 830\,\text{ksi} (0.85)(0.9) = 635\,\text{ksi} \\
\]

---

Note that \(C_P\) would also apply for column buckling of an axially loaded member.
4.32 ASD – Select Structural Southern Pine, fully braced; bending about strong axis

a. 2 x 6 joists at 24 in. o.c. \((C_r = 1.15)\); D + S load combination \((C_D = 1.15)\)

- \(C_F\) is already included in NDS Table 4B values; other factors equal to unity
- \(F_b' = F_b (C_D)(C_r) = 2550 \text{ psi} (1.15)(1.15) = 3372 \text{ psi}\)
- \(F_l' = F_l (C_D) = 1400 \text{ psi} (1.15) = 1610 \text{ psi}\)
- \(F_v' = F_v (C_D) = 175 \text{ psi} (1.15) = 201 \text{ psi}\)
- \(F_{\perp}' = F_{\perp} = 565 \text{ psi}\)
- \(F_c' = F_c (C_D) = 2000 \text{ psi} (1.15) = 2300 \text{ psi}\)

Note that \(C_p\) would also apply for column buckling of an axially loaded member.
\[E' = E = 1,800,000 \text{ psi}\]
\[E_{min}' = E_{min} = 660,000 \text{ psi}\]

b. 4 x 12 beam; D + L + L_r load combination \((C_D = 1.25)\)

- \(C_F = 1.1\) for bending; other factors equal to unity
- \(F_b' = F_b (C_D)(C_F) = 1900 \text{ psi} (1.25)(1.1) = 2613 \text{ psi}\)
- \(F_l' = F_l (C_D) = 1050 \text{ psi} (1.25) = 1313 \text{ psi}\)
- \(F_v' = F_v (C_D) = 175 \text{ psi} (1.25) = 219 \text{ psi}\)
- \(F_{\perp}' = F_{\perp} = 565 \text{ psi}\)
- \(F_c' = F_c (C_D) = 1800 \text{ psi} (1.25) = 2250 \text{ psi}\)

Note that \(C_p\) would also apply for column buckling of an axially loaded member.
\[E' = E = 1,800,000 \text{ psi}\]
\[E_{min}' = E_{min} = 660,000 \text{ psi}\]

c. 2 x 10 purlins at 4 ft o.c.; D + L_r load combination \((C_D = 1.25)\)

- \(C_F\) is already incorporated in NDS Table 4B values; other factors equal to unity
- \(F_b' = F_b (C_D) = 2050 \text{ psi} (1.25) = 2563 \text{ psi}\)
- \(F_l' = F_l (C_D) = 1100 \text{ psi} (1.25) = 1375 \text{ psi}\)
- \(F_v' = F_v (C_D) = 175 \text{ psi} (1.25) = 219 \text{ psi}\)
- \(F_{\perp}' = F_{\perp} = 565 \text{ psi}\)
- \(F_c' = F_c (C_D) = 1850 \text{ psi} (1.25) = 2313 \text{ psi}\)

Note that \(C_p\) would also apply for column buckling of an axially loaded member.
\[E' = E = 1,800,000 \text{ psi}\]
\[E_{min}' = E_{min} = 660,000 \text{ psi}\]

d. 4 x 10 beams at 4 ft o.c.; D + L + W load combination \((C_D = 1.6)\)

- \(C_F = 1.1\) for bending; other factors equal to unity
- \(F_b' = F_b (C_D)(C_F) = 2050 \text{ psi} (1.6)(1.1) = 3608 \text{ psi}\)
- \(F_l' = F_l (C_D) = 1100 \text{ psi} (1.6) = 1760 \text{ psi}\)
- \(F_v' = F_v (C_D) = 175 \text{ psi} (1.6) = 280 \text{ psi}\)
- \(F_{\perp}' = F_{\perp} = 565 \text{ psi}\)
- \(F_c' = F_c (C_D) = 1850 \text{ psi} (1.6) = 2960 \text{ psi}\)

Note that \(C_p\) would also apply for column buckling of an axially loaded member.
\[E' = E = 1,800,000 \text{ psi}\]
\[E_{min}' = E_{min} = 660,000 \text{ psi}\]
4.33 LRFD ($K_F$ and $\Phi$ apply) – Select Structural Southern Pine, fully braced; bending about strong axis

a. **2 x 6 joists** at 24 in. o.c. ($C_r = 1.15$); 1.2D + 1.6S load combination ($\lambda = 0.8$)

$C_F$ is already included in NDS Table 4B values; other factors equal to unity

$A = 8.25 \text{ in}^2$; $S_x = 7.563 \text{ in}^3$

**Bending moment**

$F_{bn} = F_b (K_F) = 2550 \text{ psi} (2.54) = 6477 \text{ psi} = 6.48 \text{ ksi}$

$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_r) = 6.48 \text{ ksi} (0.85)(0.8)(1.15) = 5.07 \text{ ksi}$

$M_n' = F_{bn}' (S_x) = 5.07 \text{ ksi} (7.563 \text{ in}^3) = 38.3 \text{ k-in.}$

**Tension**

$F_{tn} = F_t (K_F) = 1400 \text{ psi} (2.7) = 3780 \text{ psi} = 3.78 \text{ ksi}$

$F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 3.78 \text{ ksi} (0.8)(0.8) = 2.42 \text{ ksi}$

$T_n' = F_{tn}' (A) = 2.42 \text{ ksi} (8.25 \text{ in}^2) = 20.0 \text{ k}$

**Flexural Shear**

$F_{vn} = F_v (K_F) = 175 \text{ psi} (2.88) = 504 \text{ psi} = 0.504 \text{ ksi}$

$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} (0.75)(0.8) = 0.302 \text{ ksi}$

$V_n' = F_{vn}' (2/3)(A) = 0.302 \text{ ksi} (2/3)(8.25 \text{ in}^2) = 1.7 \text{ k}$

**Compression perpendicular to grain (bearing)**

$F_{cn} = F_c (K_F) = 2000 \text{ psi} (2.4) = 4800 \text{ psi} = 4.80 \text{ ksi}$

$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 4.80 \text{ ksi} (0.9)(0.8) = 3.46 \text{ ksi}$

$P_n' = F_{cn}' (A) = 3.46 \text{ ksi} (8.25 \text{ in}^2) = 28.5 \text{ k}$

*Note that $C_p$ would also apply for column buckling of an axially loaded member.*

**Modulus of Elasticity**

$E' = E = 1,800,000 \text{ psi} = 12,000 \text{ ksi}$

$E_{\text{min-n}} = E_{\text{min}} (K_F) = 660,000 \text{ psi} (1.765) = 1,165,000 \text{ psi} = 1165 \text{ ksi}$

$E_{\text{min-n}}' = E_{\text{min-n}} (\Phi_x) = 1165 \text{ ksi} (0.85) = 990 \text{ ksi}$

b. **4 x 12 beam**; 1.2D + 1.6L + 0.5L_r (occupancy) load combination ($\lambda = 0.8$)

$C_F = 1.1$ for bending; other factors equal to unity

$A = 39.38 \text{ in}^2$; $S_x = 73.83 \text{ in}^3$

**Bending moment**

$F_{bn} = F_b (K_F) = 1900 \text{ psi} (2.54) = 4826 \text{ psi} = 4.83 \text{ ksi}$

$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_F) = 4.83 \text{ ksi} (0.85)(0.8)(1.1) = 3.61 \text{ ksi}$

$M_n' = F_{bn}' (S_x) = 3.61 \text{ ksi} (73.83 \text{ in}^3) = 267 \text{ k-in.}$

**Tension**

$F_{tn} = F_t (K_F) = 1050 \text{ psi} (2.7) = 2835 \text{ psi} = 2.84 \text{ ksi}$

$F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 2.84 \text{ ksi} (0.8)(0.8) = 1.81 \text{ ksi}$

$T_n' = F_{tn}' (A) = 1.81 \text{ ksi} (39.38 \text{ in}^2) = 71.5 \text{ k}$

**Flexural Shear**

$F_{vn} = F_v (K_F) = 175 \text{ psi} (2.88) = 504 \text{ psi} = 0.504 \text{ ksi}$

$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} (0.75)(0.8) = 0.302 \text{ ksi}$

$V_n' = F_{vn}' (2/3)(A) = 0.302 \text{ ksi} (2/3)(39.38 \text{ in}^2) = 7.9 \text{ k}$
Compression perpendicular to grain (bearing)

\[ F_{c_{n'}} = F_{c_{n}} (K_F) = 565 \text{ psi} \times 2.083 = 1177 \text{ psi} = 1.177 \text{ ksi} \]

Compression parallel to grain

\[ F_{c_{n}} = F_{c} (K_F) = 1800 \text{ psi} \times 2.4 = 4320 \text{ psi} = 4.32 \text{ ksi} \]

\[ F_{c_{n'}} = F_{c_{n}} (\Phi_c)(\lambda) = 4.32 \text{ ksi} \times (0.9)(0.8) = 3.11 \text{ ksi} \]

\[ P_{n} = F_{c_{n'}} (A) = 3.11 \text{ ksi} \times 13.88 \text{ in}^2 = 122 \text{ k} \]

*Note that \( C_F \) would also apply for column buckling of an axially loaded member.*

Modulus of Elasticity

\[ E' = E = 1,800,000 \text{ psi} = 1800 \text{ ksi} \]

\[ E_{min-n} = E_{min} (K_F) = 660,000 \text{ psi} \times 1.765 = 1,165,000 \text{ psi} = 1165 \text{ ksi} \]

\[ E_{min-n'} = E_{min-n} (\Phi_s) = 1165 \text{ ksi} \times 0.85 = 990 \text{ ksi} \]

**2 \times 10 purlins** at 4 ft o.c.; 1.2D + 1.6L, load combination (\( \lambda = 0.8 \))

\( C_F \) is already incorporated in NDS Table 4B values; other factors equal to unity

\[ A = 13.88 \text{ in}^2; \ S_t = 21.39 \text{ in}^3 \]

**Bending moment**

\[ F_{bn} = F_{b} (K_F) = 2050 \text{ psi} \times 2.54 = 5207 \text{ psi} = 5.21 \text{ ksi} \]

\[ F_{bn'} = F_{bn} (\Phi_b)(\lambda) = 5.21 \text{ ksi} \times 0.85(0.8) = 3.54 \text{ ksi} \]

\[ M_{n} = F_{bn'} (S_t) = 3.54 \text{ ksi} \times 21.39 \text{ in}^3 = 75.8 \text{ k-in.} \]

**Tension**

\[ F_{tn} = F_{t} (K_F) = 1100 \text{ psi} \times 2.7 = 2970 \text{ psi} = 2.97 \text{ ksi} \]

\[ F_{tn'} = F_{tn} (\Phi_t)(\lambda) = 2.97 \text{ ksi} \times (0.8)(0.8) = 1.90 \text{ ksi} \]

\[ T_{n} = F_{tn'} (A) = 1.90 \text{ ksi} \times 13.88 \text{ in}^2 = 26.4 \text{ k} \]

**Flexural Shear**

\[ F_{vn} = F_{v} (K_F) = 175 \text{ psi} \times 2.88 = 504 \text{ psi} = 0.504 \text{ ksi} \]

\[ F_{vn'} = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} \times 0.75(0.8) = 0.302 \text{ ksi} \]

\[ V_{n} = F_{vn'} (2/3)(A) = 0.302 \text{ ksi} \times (2/3)(13.88 \text{ in}^2) = 2.8 \text{ k} \]

Compression perpendicular to grain (bearing)

\[ F_{c_{n}} = F_{c} (K_F) = 565 \text{ psi} \times 2.083 = 1177 \text{ psi} = 1.177 \text{ ksi} \]

\[ F_{c_{n'}} = F_{c_{n}} (\Phi_c)(\lambda) = 1.177 \text{ ksi} \times (0.9)(0.8) = 0.847 \text{ ksi} \]

Compression parallel to grain

\[ F_{c_{n}} = F_{c} (K_F) = 1850 \text{ psi} \times 2.4 = 4440 \text{ psi} = 4.44 \text{ ksi} \]

\[ F_{c_{n'}} = F_{c_{n}} (\Phi_c)(\lambda) = 4.44 \text{ ksi} \times (0.9)(0.8) = 3.20 \text{ ksi} \]

\[ P_{n} = F_{c_{n'}} (A) = 3.20 \text{ ksi} \times 13.88 \text{ in}^2 = 44.4 \text{ k} \]

*Note that \( C_F \) would also apply for column buckling of an axially loaded member.*

Modulus of Elasticity

\[ E' = E = 1,800,000 \text{ psi} = 1800 \text{ ksi} \]

\[ E_{min-n} = E_{min} (K_F) = 660,000 \text{ psi} \times 1.765 = 1,165,000 \text{ psi} = 1165 \text{ ksi} \]

\[ E_{min-n'} = E_{min-n} (\Phi_s) = 1165 \text{ ksi} \times 0.85 = 990 \text{ ksi} \]
d. **4 x 10 beams** at 4 ft o.c.; 1.2D + 1.6W + L load combination (λ = 1.0)

\[ C_F = 1.1 \text{ for bending; other factors equal to unity} \]

\[ A = 32.38 \text{ in}^2; S_t = 49.91 \text{ in}^3 \]

**Bending moment**

\[ F_{bn} = F_b (K_F) = 2050 \text{ psi} (2.54) = 5207 \text{ psi} = 5.21 \text{ ksi} \]

\[ F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_F) = 5.21 \text{ ksi} (0.85)(1.0)(1.1) = 4.87 \text{ ksi} \]

\[ M_n' = F_{bn}' (S_t) = 4.87 \text{ ksi} (49.91 \text{ in}^3) = 243 \text{ k-in.} \]

**Tension**

\[ F_{tn} = F_t (K_F) = 1100 \text{ psi} (2.7) = 2970 \text{ psi} = 2.97 \text{ ksi} \]

\[ F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 2.97 \text{ ksi} (0.8)(1.0) = 2.38 \text{ ksi} \]

\[ T_n' = F_{tn}' (A) = 2.38 \text{ ksi} (32.38 \text{ in}^2) = 76.9 \text{ k} \]

**Flexural Shear**

\[ F_{vn} = F_v (K_F) = 175 \text{ psi} (2.88) = 504 \text{ psi} = 0.504 \text{ ksi} \]

\[ F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} (0.75)(1.0) = 0.378 \text{ ksi} \]

\[ V_n' = F_{vn}' (2/3)(A) = 0.378 \text{ ksi} (2/3)(32.38 \text{ in}^2) = 8.2 \text{ k} \]

**Compression perpendicular to grain (bearing)**

\[ F_{cn} = F_c (K_F) = 1850 \text{ psi} (2.4) = 4440 \text{ psi} = 4.44 \text{ ksi} \]

\[ F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 4.44 \text{ ksi} (0.9)(1.0) = 4.00 \text{ ksi} \]

\[ P_n' = F_{cn}' (A) = 4.00 \text{ ksi} (32.38 \text{ in}^2) = 129 \text{ k} \]

*Note that C_F would also apply for column buckling of an axially loaded member.*

**Modulus of Elasticity**

\[ E' = E = 1,800,000 \text{ psi} = 1800 \text{ ksi} \]

\[ E_{min-n} = E_{min} (K_F) = 660,000 \text{ psi} (1.765) = 1,165,000 \text{ psi} = 1165 \text{ ksi} \]

\[ E_{min-n}' = E_{min-n} (\Phi_s) = 1165 \text{ ksi} (0.85) = 990 \text{ ksi} \]
4.34 \( SV = \frac{6}{30} = 0.2\% \) per 1% change in MC = 0.002 in./in./percent change in MC
\[ \Delta MC = 10 - 19 = -9 \text{ (drying)} \]
Shrinkage = \( SV(\Delta MC) \times d = (0.002)(-9)(13.25 \text{ in.}) = 0.24 \text{ in.} \)
Depth after shrinkage = 13.25 – 0.24 in. = 13 in.

4.35 \( SV = \frac{6}{30} = 0.2\% \) per 1% change in MC = 0.002 in./in./percent change in MC
\[ \Delta MC = 9 - 19 = -10 \text{ (drying)} \]
Shrinkage in 2 x 10 = \( SV(\Delta MC) \times d = (0.002)(-10)(9.25 \text{ in.}) = 0.185 \text{ in.} \)
Shrinkage in 2 x plate = \( SV(\Delta MC) \times d = (0.002)(-10)(1.5 \text{ in.}) = 0.03 \text{ in.} \)
three 2 x 12’s; twelve 2 x plates
Total shrinkage = 3(0.185 in.) + 12(0.03 in.) = 0.9 in.